

28. A population of rabbits grows in such a way that the population t days from now is given by

$$A(t) = 250e^{0.02t}$$

a. What is the current rabbit population? \rightarrow at $t = 0$

$$A(0) = 250e^{0.02(0)} = 250$$

b. How many rabbits will there be after 4 days?

$$= 250e^{0.02(4)} = 270.82 \approx 271$$

c. How many rabbits will there be after three weeks?

$$= 250e^{0.02(21)} = 380.49 \approx 380$$

** d. How many days will it take for the rabbit population to double? ** This means for the initial population to double!

$$500 = 250e^{0.02t} \rightarrow \ln 2 = \ln e^{0.02t} \rightarrow \frac{\ln 2}{0.02} = \frac{0.02t}{0.02} \rightarrow t = 34.657 \text{ days}$$

29. Write an exponential function of the form $y = ab^x$ whose graph passes through the given points.

a. (0, 5) and (1, 15)

$$5 = ab^0 \quad 15 = 5(b)^1 \quad y = 5 \cdot 3^x$$

$$5 = a(1) \quad \frac{15}{5} = \frac{5(b)}{5} \quad 3 = b$$

$$5 = a \quad 3 = b$$

b. (0, 20) and (2, 500)

$$20 = ab^0 \quad \frac{500}{20} = \frac{20b^2}{20} \quad y = 20 \cdot 5^x$$

$$20 = a \cdot 1 \quad 25 = b^2$$

$$20 = a \quad \pm 5 = b$$

30. Starting with the graph of $f(x) = 4^x$, write the equation of the graph that results from

a. Shifting $f(x)$ 4 units upwards

$$f(x) = 4^x + 4$$

c. Shifting $f(x)$ 2 units left

$$f(x) = 4^{x+2}$$

e. Reflecting $f(x)$ about the x-axis

$$f(x) = -1 \cdot 4^x$$

b. Shifting $f(x)$ 3 units downwards

$$f(x) = 4^x - 3$$

d. Shifting $f(x)$ 5 units right

$$f(x) = 4^{x-5}$$

f. Reflecting $f(x)$ about the y-axis

$$f(x) = 4^{-x}$$

31. Match each equation with one of the graphs below:

B a. $f(x) = 2(0.69)^x$

F b. $f(x) = 2(1.28)^x$

A c. $f(x) = 2(0.81)^x$

D d. $f(x) = 4(1.28)^x$

E e. $f(x) = 2(1.59)^x$

C f. $f(x) = 4(0.69)^x$

